

<<紧李群>>

图书基本信息

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内容概要

塞潘斯基编著的《紧李群（影印版）》是“国外数学名著系列”之一，内容包括紧李群、群表示论、调和分析、李代数、阿贝尔李子群等。

可供高等院校数学专业研究生、数学类科研人员学习参考。

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